

KEY STAGE

ALL TIERS

Mathematics tests **Mark scheme** for Paper 1 Tiers 3–5, 4–6, 5–7 and 6–8



National curriculum assessments

https://www.SATs-Papers.co.uk

Introduction

This booklet contains the mark scheme for paper 1 at all tiers. The paper 2 mark scheme is printed in a separate booklet. Questions have been given names so that each one has a unique identifier irrespective of tier.

The structure of the mark schemes

The marking information for each question is set out in the form of tables, which start on page 10 of this booklet. The columns on the left-hand side of each table provide a quick reference to the tier, question number, question part and the total number of marks available for that question part.

The 'Correct response' column usually includes two types of information:

- a statement of the requirements for the award of each mark, with an indication of whether credit can be given for correct working, and whether the marks are independent or cumulative
- examples of some different types of correct response, including the most common.

The **'Additional guidance'** column indicates alternative acceptable responses, and provides details of specific types of response that are unacceptable. Other guidance, such as when 'follow-through' is allowed, is provided as necessary.

Questions with a Using and applying mathematics (UAM) element are identified in the mark scheme by the symbol (U1). The number indicates the significance of using and applying mathematics in answering the question. The U number can be any whole number from 1 to the number of marks in the question.

For graphical and diagrammatic responses, including those in which judgements on accuracy are required, marking overlays have been provided as the centre pages of this booklet.

The 2009 key stage 3 mathematics tests and mark schemes were developed by the Test Development Team at Pearson Research and Assessment.

General guidance

Using the mark schemes

Answers that are numerically equivalent or algebraically equivalent are acceptable unless the mark scheme states otherwise.

In order to ensure consistency of marking, the most frequent procedural queries are listed on the following two pages with the prescribed correct action. This is followed by further guidance relating specifically to the marking of questions that involve money, negative numbers, time, measures, coordinates, probability or algebra. Unless otherwise specified in the mark scheme, markers should apply the following guidelines in all cases.

Recording marks awarded on the test paper

All questions, even those not attempted by the pupil, should be marked, with a 1 or a 0 entered in each marking space. Where 2m can be split into 1m gained and 1m lost, with no explicit order, then this will be recorded by the marker as 1

The total marks awarded for a double page should be written in the box at the bottom of the right-hand page, and the total number of marks obtained on the paper should be recorded on the front of the test paper.

A total of 120 marks is available in each of tiers 3–5, 4–6, 5–7 and 6–8.

Awarding levels

The sum of the marks gained on paper 1, paper 2 and the mental mathematics paper determines the level awarded. Level threshold tables, which show the mark ranges for the award of different levels, will be available on the NAA website *www.naa.org.uk/tests* from April 2009.

What if	Marking procedure		
The pupil's response is numerically or algebraically equivalent to the answer in the mark scheme.	y n		
The pupil's response does not match closely any of the examples given.	Markers should use their judgement in deciding whether the response corresponds with the statement of the requirements given in the 'Correct response' column. Refer also to the 'Additional guidance'.		
The pupil has responded in a non-standard way.	Calculations, formulae and written responses do not have to be set out in any particular format. Pupils may provide evidence in any form as long as its meaning can be understood. Diagrams, symbols or words are acceptable for explanations or for indicating a response. Any correct method of setting out working, however idiosyncratic, should be accepted. Provided there is no ambiguity, condone the continental practice of using a comma for a decimal point.		
There appears to be a misreading affecting the working.	This is when the pupil misreads the information given in the question and uses different information without altering the original intention or difficulty level of the question. For each misread that occurs, deduct one mark only.		
No answer is given in the expected place, but the correct answer is given elsewhere.	Where a pupil has shown understanding of the question, the mark(s) should be given. In particular, where a word or number response is expected, a pupil may meet the requirement by annotating a graph or labelling a diagram elsewhere in the question.		
The final answer is wrong, but the correct answer is shown in the working.	Where appropriate, detailed guidance will be given in the be adhered to. If no guidance is given, markers will need to decide whether:		
	• the incorrect answer is due to a transcription error	If so, award the mark.	
	 in questions not testing accuracy, the correct answer has been given but then rounded or truncated 		
	• the pupil has continued to give redundant extra If so, award the m working which does not contradict work already done		
	• the pupil has continued, in the same part of the question, to give redundant extra working which does contradict work already done.	If so, do not award the mark. Where a question part carries more than one mark, only the final mark should be withheld.	
The pupil's answer is correct but the wrong working is shown. A correct response should always be marked as correct unless the mark scheme states otherwise.			

What if	Marking procedure		
The pupil has made a conceptual error.	In some questions, a method mark is available provided the pupil has made a computational, rather than conceptual, error. A computational error is a 'slip' such as writing $4 \times 6 = 18$ in an otherwise correct long multiplication. A conceptual error is a more serious misunderstanding of the relevant mathematics; when such an error is seen, no method marks may be awarded. Examples of conceptual errors are:		
	- misunderstanding of place value, such as multiplying by 2 rather than 20 when calculating 35 \times 27		
	 subtracting the smaller value from the larger in calculations such as 45 – 26 to give the answer 21 		
	• incorrect signs when working with negative numbers.		
The correct response has been crossed or rubbed out and not replaced.	Any legible crossed or rubbed out work that has not been replaced should be marked according to the mark scheme. If the work is replaced, then crossed or rubbed out work should not be considered.		
More than one answer is given.	If all answers given are correct (or a range of answers is given, all of which are correct), the mark should be awarded unless prohibited by the mark scheme. If both correct and incorrect responses are given, no mark should be awarded.		
The pupil's answer correctly follows through from earlier incorrect work.	Follow-through marks may be awarded only when specifically stated in the mark scheme, but should not be allowed if the difficulty level of the question has been lowered. Either the correct response or an acceptable follow-through response should be marked as correct.		
The answer is correct but, in a later part of the question, the pupil has contradicted this response.	A mark given for one part should not be disallowed for working or answers given in a different part, unless the mark scheme specifically states otherwise.		
The pupil's accuracy is marginal according to the overlay provided.	Overlays can never be 100% accurate. However, provided the answer is within or touches the boundaries given, the mark(s) should be awarded.		
The pupil has drawn lines which do not meet at the correct point.	Markers should interpret the phrase 'lines not accurate' to mean meeting within or on a circle of radius 2mm with centre at the correct point. $\begin{array}{c} \hline \\ \hline $		

Responses involving money

	✓ Accept	× Do not accept
Where the £ sign is given for example: £3.20, £7	 ✓ f3.20 f7 f7.00 Any unambiguous indication of the correct amount, eg f3.20p f3 20 pence f3 20 f3.20 f3.20 f3.20 f3.20 f3.20 f3.20 f3.20 gamma for the sign crossed out 	 Incorrect placement of pounds or pence, eg f320 f320p Incorrect placement of decimal point, or incorrect use or omission of 0, eg f3.2 f3 200 f32 0 f3-2-0
Where the p sign is given for example: 40p	 ✓ 40p Any unambiguous indication of the correct amount, eg f0.40p f.40p f0.40 with p sign crossed out 	 Incorrect or ambiguous use of pounds or pence, eg 0.40p £40p
Where no sign is given for example: £3.20, 40p	 ✓ f3.20 320p 40p f0.40 Any unambiguous indication of the correct amount in f or p as shown above At levels 3 and 4 only also accept omission of units, eg 3.20 320 40 0.40 	 Comission of final zero, eg 3.2 0.4

Responses involving negative numbers

	✓ Accept	× Do not accept
For example: -2		To avoid penalising the error below more than once within each question, do not award the mark for the <i>first</i> occurence of the error within each question. Where a question part carries more than one mark, only the final mark should be withheld. Incorrect notation, eg 2-

Responses involving time

	✓ Accept	× Do not accept
A time interval for example: 2 hours 30 minutes	 ✓ 2 hours 30 minutes Any unambiguous, correct indication, eg 2¹/₂ hours 2.5 hours 2.6 hours 2.6 hours 2.7 hours 2.8 no 2.8 no	 Incorrect or ambiguous time interval, eg 2.3 hours 2.3h 2h 3 2.30 min 2.30 2.30 2.30 2.30 2.30
A specific time for example: 8:40am, 17:20	 ✓ 8:40am 8:40 twenty to nine Any unambiguous, correct indication, eg 08.40 8.40 0840 8.40 0840 8.40 Unambiguous change to 12 or 24 hour clock, eg 17:20 as 5:20pm or 17:20pm 	 Incorrect time, eg 8.4am 8.40pm Incorrect placement of separators, spaces, etc or incorrect use or omission of 0, eg 840 8:4:0 8:4 084 84

Responses involving measures

	✓ Accept	× Do not accept
Where units are given (eg kg, m, l) for example: 8.6kg	 ✓ 8.6kg Any unambiguous indication of the correct measurement, eg 8.60kg 8.6000kg 8kg 600g 	 Incorrect or ambiguous use of units, eg 8600kg

Note

If a pupil leaves the answer box empty but writes the answer elsewhere on the page, then that answer must be consistent with the units given in the answer box and the conditions listed above.

If a pupil changes the unit given in the answer box, then their answer must be equivalent to the correct answer, using the unit they have chosen, unless otherwise indicated in the mark scheme.

Responses involving coordinates

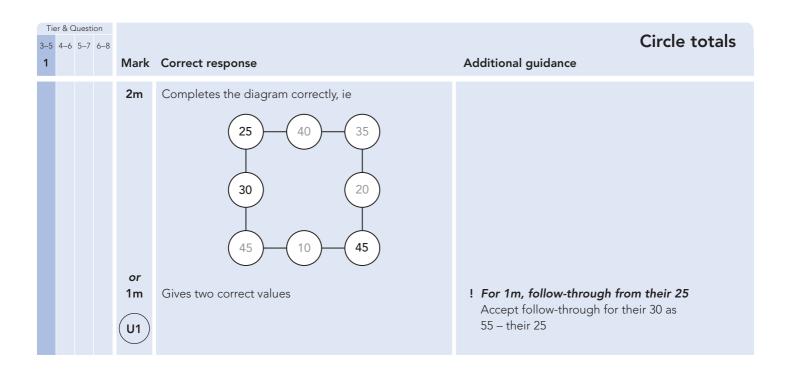
	✓ Accept	× Do not accept
For example: (5, 7)	✓ Unconventional notation, eg (05, 07) (five, seven) x y (5, 7) (x=5, y=7)	✓ Incorrect or ambiguous notation, eg (7, 5) y x (7, 5) (5x, 7y) (5 ^x , 7 ^y) (x−5, y−7)

Responses involving probability

	✓ Accept	! Take care × Do not accept
A numerical probability should be expressed as a decimal, fraction or percentage only. for example: $0.7 \frac{7}{10} 70\%$	 ✓ Equivalent decimals, fractions and percentages, eg 0.700	The first four categories of error below should be ignored if accompanied by an acceptable response, but should not be accepted on their own. However, to avoid penalising the first three types of error below more than once within each question, do not award the mark for the <i>first</i> occurrence of each type of error unaccompanied by an acceptable response. Where a question part carries more than one mark, only the final mark should be withheld.
	✓ A probability correctly expressed in one acceptable form which is then incorrectly converted, but is still less than 1 and greater than 0, eg $\frac{70}{100} = \frac{18}{25}$	 A probability that is incorrectly expressed, eg 7 in 10 7 over 10 7 out of 10 7 from 10 A probability expressed as a percentage without a percentage sign. A fraction with other than integers in the numerator and/or denominator. A probability expressed as a ratio, eg 7:10 7:3 7 to 10 A probability greater than 1 or less than 0

Responses involving the use of algebra

	✓ Accept	! Take care × Do not accept
For example: 2 + n n + 2 2n $\frac{n}{2}$ n^2	 ✓ Unambiguous use of a different case or variable, eg N used for n x used for n 	! Unconventional notation, eg $n \times 2$, or $2 \times n$, or $n2$ or $n + n$ for $2n$ $n \times n$ for n^2 $n \div 2$ for $\frac{n}{2}$ or $\frac{1}{2}n$ 2 + 1n for $2 + n2 + 0n$ for $2Within a question that demandssimplification, do not accept as part ofa final answer involving algebra. Acceptwithin a method when awarding partialcredit, or within an explanation orgeneral working.$
		Embedded values given when solving equations, eg in solving $3x + 2 = 32$, $3 \times 10 + 2 = 32$ for $x = 10$ To avoid penalising the two types of error below more than once within each question, do not award the mark for the <i>first</i> occurrence of each type within each question. Where a question part carries more than one mark, only the final mark should be withheld.
	✓ Words used to precede or follow equations or expressions, eg t = n + 2 tiles or tiles = $t = n + 2for t = n + 2$	 Words or units used within equations or expressions, eg n tiles + 2 n cm + 2 Do not accept on their own. Ignore if accompanying an acceptable response.
	✓ Unambiguous letters used to indicate expressions, eg t = n + 2 for $n + 2$	Ambiguous letters used to indicate expressions, eg n = n + 2 for $n + 2$





	Question 5 5-7 6-8			Dishes
2		Mark	Correct response	Additional guidance
а		1m	£11	
b		2m or 1m	f2.50 Gives the answer 2.5 or 250 or Shows the value 7.5(0) or 750 or Shows or implies a complete correct method with not more than one computational error eg • $1.50 + 2.50 + 3.50 = 7.00$ (error) Answer given as 3	
C		1m 1m (U1)	Gives a correct pair of colours, in any order, ie Green and Orange or Blue and Red Gives a correct pair of colours, other than any previously credited	 ✓ Unambiguous indication of colour eg G and O B and R I Response gives costs rather than colours Withhold 1 mark only for the first occurrence. Allow costs given in pence eg 1.50 and 3(.00) 2(.00) and 2.50 150 and 300 200 and 250 Mark as 0, 1

	er & Question 4–6 5–7 6–8		Correct response	Five squares
а		1m	Draws the correct line of symmetry, ie	! Line not ruled, accurate or extended Accept lines of at least 3 diagonals in length provided the pupil's intention is clear
b		1m	Completes the diagram correctly, ie	! Squares not shaded Accept provided indication of squares is unambiguous

	ier & Qu 4–6	uestion 5–7 6–8			Javelin
4				Correct response	Additional guidance
а			1m	16 to 18 inclusive	
b			1m	4	
с			1m	17 to 19 inclusive	



Tier & Question 3–5 4–6 5–7 6–8		Digit cards
5 Ma	ark Correct response	Additional guidance
1r	 m Gives four of the digits to make a correct calculation eg 7 + 8 = 15 5 + 6 = 11 9 + 9 = 18 	 ! Zero used at the end of a number eg, for the first mark 2 + 8 = 10 Penalise only the first occurrence * Zero used or card left blank at the
1r	 m Gives four of the digits to make a correct calculation eg 6 × 7 = 42 7 × 5 = 35 9 × 9 = 81 	 beginning of a two-digit number eg, for the second mark, do not accept 2 × 3 = 06 Card left blank at the end of a number cg for the third mark, do not accept
1r	 m Gives five of the digits to make a correct calculation eg 23 - 4 = 19 67 - 5 = 62 24 - 2 = 22 	 eg, for the third mark, do not accept 2-1=1 <i>Extra digit inserted</i> eg, for the fourth mark, do not accept 36 ÷ 2 = 18
1r U	Gives four of the digits to make a correct calculation eg • $14 \div 2 = 7$ • $24 \div 4 = 6$ • $36 \div 6 = 6$	

	er & Question 4–6 5–7 6–8		Correct response	Heights Additional guidance
а		1m	Indicates 1.8 metres, ie	
b		1m	Indicates 7 metres, ie	

Tier & Question 3-5 4-6 5-7 6-8 7 Ma	ark Co	rrect response				Additional guidance	Change
a 1r	m 3						
b 2r o 1r	an <u>;</u> eg •	Number of 50p coins 2 2 2 2 2 2 mpletes two roo	Number of 20p coins 3 2 1 0	Number of 10p coins 0 2 4 6	n	✓ Cell that should contain zero lef	it blank

	Tier & Question		on			Destaur	
3	-5	4–6	5–7	6–8			Doctors
1	B	1			Mark	Correct response	Additional guidance
	a D	a b			1m 1m	Gives a value between 49 and 53 inclusive Gives a value between 23 and 27 inclusive	 ✓ Value qualified eg, for part (a) • About 50
	C	c			1m	 Gives a possible reason eg They might think their doctor's treatment is sometimes very good, but not at other times They might not think that any of the possible answers is what they think They don't have a doctor They might not want to comment They could be worried about giving an opinion They may have only ever had one doctor They don't always see the same doctor 	 Minimally acceptable reason eg Could be sometimes one category and sometimes another They may not like the choices If they're not sure They don't see their doctor very often They have just got a new doctor Not relevant They don't want to answer They can't tell what is meant by good Incomplete reason eg They don't know

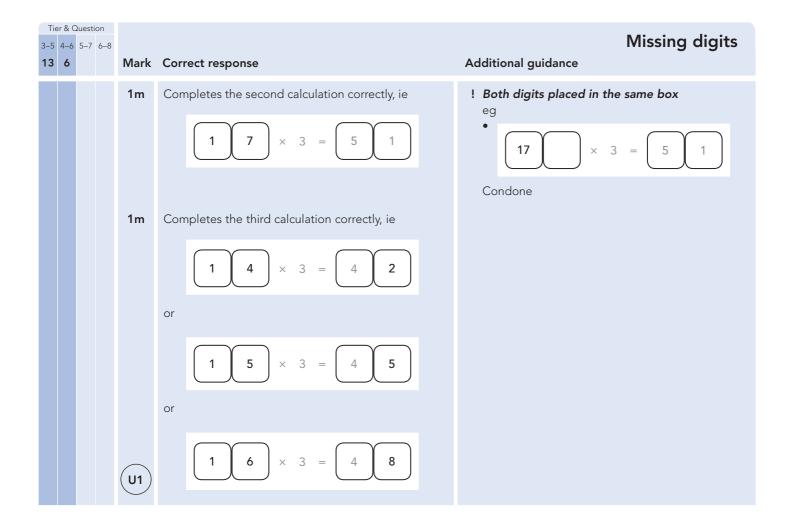
3-	-5		ion 6–8		Correct response	Using tens Additional guidance
					÷ 10 ÷ 10 → - 10	 Correct operation indicated, but 10 omitted eg, for the first mark ÷
				1m	+ 10> ÷ 10	Penalise only the first occurrence

10 3 Mark Correct response Additional guidance Image: Second secon	Tier & Question 3–5 4–6 5–7 6–8			Card shape
or Indicates any two of the correct shapes with the third incorrect or omitted or Indicates the three correct shapes with not more than		Mark	Correct response	Additional guidance
Condone		or	Indicates any two of the correct shapes with the third incorrect or omitted or Indicates the three correct shapes with not more than	eg • ✓ for yes and x for no ! For 1 mark, response indicates only the three shapes showing the grey side of the shape, eg

	ier & 1	ion 6–8			Number lines
1	4		Mark	Correct response	Additional guidance
			1m	Gives both the values 2 and 8 in the correct positions	
			1m	Gives the value –4 in the correct position	
			1m	Gives the value (+)6 in the correct position	 Follow-through from their -4 Accept the sum of their -4 and 10 provided their -4 is a negative number

2009 KS3 Mathematics test mark scheme: Paper 1

3–5		Questi 5−7	Mark	Correct response	Rhombus grid
а	а		1m	12	
b	b		1m	Draws a correct triangle eg • • • • • • • • • • • • • • • • • • •	 Lines not ruled or accurate, or triangle not shaded Accept provided the pupil's intention is clear Vertices of triangle not on the intersections of the grid Accept vertices within 2mm of the intersections of the grid Other shapes drawn As these may be trials, ignore



Tie	r & Q	uestior	١		
3–5	4–6	5–7 6	-8		Clocks
14	7		Mar	k Correct response	Additional guidance
а	а		1m	10am	! Indication of am or pm incorrect or omitted Condone omission of am or pm but do not
b	Ь		1m	брт	accept incorrect times eg, for part (a) accept 10 (o'clock) eg, for part (a) do not accept 10pm 22:00 eg, for part (b) accept 6 (o'clock) 18:00 eg, for part (b) do not accept 6am 06:00

Tier & Question 3-5 4-6 5-7 6-8 15 8 Mark	Correct response	Sum of 80 Additional guidance
1m (U1)	 Indicates Set A and gives a correct explanation eg A = 74 and 80 - 74 = 6 B = 90 and 90 - 80 = 10 A is -3, -2, -1, (0) and B is +1, +2, +3, +4, so A is only 6 less than 80, but B is 10 more 	 ✓ Minimally acceptable explanation eg 6 and 10 seen 74 and 90 seen (-)3, (-)2, (-)1, (0) and 1, 2, 3, 4 seen ✓ Incomplete or incorrect explanation eg A adds up to 74 B is 10 more than 80 A adds up to 74, B adds up to 110 17, 18 and 19 are all under 20 so A is smaller

	ier & (Number chains
10	5 9		Mark	Correct response	Additional guidance
а	а		1m	Gives the values 14 and 41 in the correct positions	
b	b		1m	Shows a correct rule eg • × 3 • Multiply by 3 • Triple • × 3 then + 0	 ✓ Minimally acceptable rule eg Add the number 3 times Add on double itself Double then add the number It's the next power of 3 3× I Rule embedded or shown in working Accept provided a correct rule is shown explicitly, even if an incorrect value for the next number in the chain is shown on the answer line eg, accept 81 × 3 seen (4 - 1) × 81 eg, do not accept 81 + 81 + 81 81 × 2 + 81 <i>Incomplete or incorrect rule</i> eg 3 +54 3n

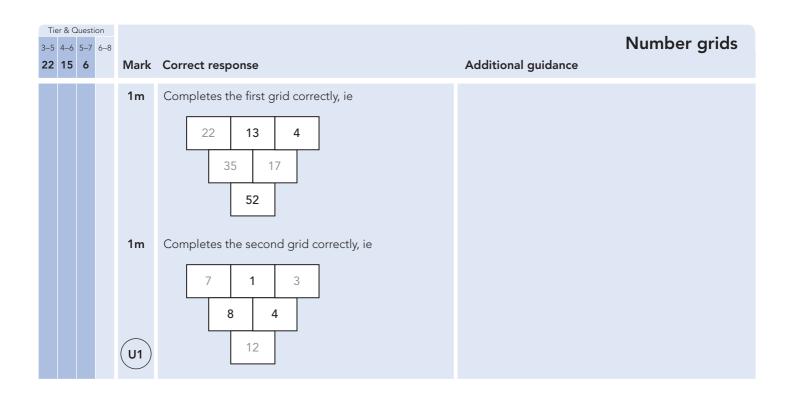
3–5		Duestio 5–7 d 1	5-8	Mark	Correct response	Making 1 Additional guidance
а	а	a		or 1m	Joins all four pairs of numbers correctly, ie 0.1 0.99 0.11 0.9 0.01 0.999 0.01 0.999 0.91 0.89 0.001 0.09 Joins at least two pairs of numbers correctly	➤ Number matched to more than one other For 2m or 1m, do not accept as a correct match
Ь	b	b		2m or 1m	Joins all four pairs of numbers correctly, ie 1 2 0.5 4 0.25 1 0.1 20 0.05 10 Joins at least two pairs of numbers correctly	

	ier & C				T-shirts
18	11	2	Mark	Correct response	Additional guidance
а	а	а	1m	$\frac{1}{5}$ or equivalent probability	
b	b	b	1m	$\frac{2}{3}$ or equivalent probability	! Value rounded Accept 0.66() or 0.67 or the percentage equivalents
с	с	с	1m	$\frac{1}{3}$ or equivalent probability	! Value rounded Accept 0.33() or the percentage equivalent

	Duestion 5–76 3	-8	Correct response	Water Additional guidance
		1m (U1)	Indicates the value 500 on the jug, ie millilitres 1000 800 600 400 200	 ✓ Unambiguous indication ! Inaccurate indication Accept provided the pupil's intention is clear

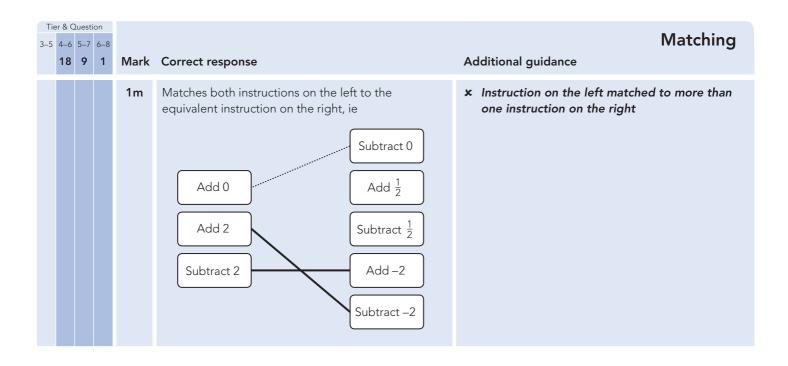
3–5	2uestio 5–7 4	Mark	Correct response	Additional guidance	Boxes
		2m or 1m	 90 Shows or implies a complete correct method with not more than one computational error eg 72 ÷ 4 = 16 (error) 72 + 16 = 88 72 ÷ 4 = 18 18 × 5 = 80 (error) 		

Т	Tier & Question				Deveentervee	
3-5 21	4–6 14		6–8	Mark	Correct response	Additional guidance
a	a	а		1m	18	 Throughout the question, incorrect use of % sign eg 18% 54% Penalise only the first occurrence
b	b	b		1m	54	 For part (b) follow-through Accept follow-through as their (a) × 3, or as 36 + their (a) provided the result is less than 360



3–5	4-6	Questio 5–7	Moule	Connect very enco	Angles in a triangle
23	16	1	Wark	Correct response	Additional guidance
			3m or	Gives all three correct angles, ie x = 90 y = 20 z = 20	
			2m or	Gives any two correct angles or Gives $x = 90$ and $y = z$, provided this value is < 90 and > 0	
			1m	Gives any one correct angle or Gives $y = z$, provided this value is < 90 and > 0	

3-5	2uestio 5–7 α 8	Mark	Correct response	Finding $m{b}$ Additional guidance
		2m or 1m	2 Shows or implies that $a = 5$ and shows the intention to substitute this value into the second equation eg • $5 + 7 = 10 + b$ • $b = 12 - 10$ or Shows a complete correct method with not more than one computational error eg • $b = 11 - 6 + 7 - 10$ • $a = 11 - 6 = 6$ (error) 6 + 7 = 10 + b b = 3	 Conceptual error eg a = 11 + 6 = 17



Tier & C 3–5 4–6				Oak leaves
	2	Mark	Correct response	Additional guidance
		1m (U1)	 Gives a correct reason from one of the five categories below that states or implies the problem, or suggests an improvement The most common correct reasons: Category 1: Refer to the number of leaves in the sample being too small eg, problem The sample is too small Those 10 leaves might all be diseased eg, improvement They should pick more than 10 Category 2: Refer to the number of trees in the sample being too small eg, problem One oak tree might be different from others May be something wrong with that tree eg, improvement They should use more than one tree Category 3: Refer to the conditions in which the tree is growing being too uniform eg, problem Different conditions may affect the leaves on other trees The soil might be very bad in that area eg, improvement They should choose trees in different areas Category 4: Refer to the area of the tree from which the leaves are picked being too small eg, problem The leaves on higher branches might be different The son higher branches might be different The son higher branches might be different The leaves from all over the tree Category 5: Refer to the period for picking the sample being too short eg, problem The leaves may be different at different times of year It may be winter eg, improvement The leaves may be different at different times of year 	 Minimally acceptable reason eg, problem Too small Only 10 Not enough Just one Same growing conditions for the tree Other branches might be different Only the lowest branches eg, improvement 100 is better More than one Need different areas Use other branches Collect at other times For the first or the second reason, more than one reason given within one response Do not accept a correct response accompanied by an incorrect response from the same category. Otherwise ignore irrelevant or incorrect further responses. If two correct reasons from different categories are given in one response space, both marks should be awarded eg They need more trees from more areas Mark as 1, 1 Incomplete reason that repeats the information given with no further explanation eg They are taking 10 leaves They are taking them from one part of the tree

Tier & Question 3-5 4-6 5-7 6-8			Missing lengths
20 11 3 Mark	Correct response	Additional guidance	
2m or 1m	Gives both correct lengths, ie x = 10 and $y = 3.9$ or equivalent Gives $y = 3.9$ or equivalent or Gives the two values transposed, ie x = 3.9 or equivalent and $y = 10orShows a complete correct method with not morethan one computational erroreg• x = 10, 10 - 6.1 = 4.9 (error)• 4 \times 6.1 = 24.4, 40 - 24.4 = 16.6 (error)16.6 \div 4 = 4.15, 4.15 + 6.1 = 10.25$		
	Gives the two values transposed, ie x = 3.9 or equivalent and $y = 10orShows a complete correct method with not morethan one computational erroreg• x = 10, 10 - 6.1 = 4.9 (error)• 4 \times 6.1 = 24.4, 40 - 24.4 = 16.6 (error)$		

	Tier & Question -5 4-6 5-7 6-8				Counters	
3–5		5-7 12		Mark	Correct response	Additional guidance
	a	a	a	2m or 1m	Gives the value 3, with no evidence of an incorrect method Shows or implies a correct equation for the bags and shows or implies a correct first step of algebraic manipulation that either reduces the number of terms or collects variables on one side of the equation and numbers on the other eg • $6y + 1 = 4y + 7$ 6y - 4y = 7 - 1 • $-2y + 7 = 1$ • $6y - 6 = 4y$ • $2y = 6$! Method used is trial and improvement Note that no partial credit can be given
	b	b	Ь	2m or 1m	5 Gives an answer of 4.() or Shows or implies a correct inequality using the expressions for the bags eg • $4k > k + 12$ • $3k > 12$ • $k > 4$! Method used is trial and improvement Note that no partial credit can be given

r & Ques			Prize money
4–6 5–7 22 13	Mark	Correct response	Additional guidance
	2m	£ 490 000	√ £ 490k
	or 1m	Shows the value 980 000	
		or	
		Shows a complete correct method with not more than one error	 For 1m, one million taken to be 100 000
		eg	• 100 000 - 20 000 = 80 000,
		 1 000 000 - 20 000 = 98 000 (error), 98 000 ÷ 2 = 49 000 	80 000 ÷ 2 = 40 000
			 For 1m, computational error that simplifies the division
			eg • 1 000 000 – 20 000 = 800 000,
			800 000 ÷ 2 = 400 000

3–5	4–6		6–8			Correlation
	23	14	6	Mark	Correct response	Additional guidance
	a	а	a	1m	 Indicates B and gives a correct explanation The most common correct explanations: Refer to the 'slope' or 'gradient' of the points eg The points make a pattern that is sloping upwards from left to right The line of best fit would have a positive gradient Describe the relationship between the two variables eg As the value on the <i>x</i>-axis increases, so does the value on the <i>y</i>-axis 	 Minimally acceptable explanation eg
	b	b	b	1m	 Indicates A and gives a correct explanation The most common correct explanations: Refer to the points being closer to a line of best fit eg The points are practically in a straight line, so the correlation is very strong If you drew the line of best fit, the points in A would all be close to it but many would be further away in B Refer to the 'line' or sloping pattern being clearer to see eg You can see the pattern of a very clear, almost straight line In B you can see a pattern sloping upward, but it's not as clear 	 Minimally acceptable explanation eg • They are closer to one line • In B they are less bunched together in a line Incomplete explanation eg • The points are closer together • In B they are more spread out Minimally acceptable explanation eg • They are in a straight line • The pattern sloping downwards is clear • In B the line is less easy to see • B's points are sloping upwards, but not as definitely as in A Incomplete explanation eg • The pattern is clearer • They are in a line

Tier & Question 3-5 4-6 5-7 6-8		Shape rules
24 15 7 Mark	Correct response	Additional guidance
2m	Completes all three rules correctly, ie $H = \underline{N} + 1$ $A = \underline{H} \times 2$ $\underline{A} = 2N + 2$! Throughout the question, unconventional notation eg, for the first rule 1N+1 Condone ! Throughout the question, words used instead of letters eg, for the second rule A = <u>Height</u> × 2 Penalise only the first occurrence ! For the second rule, N + 1 used Accept provided there is no ambiguity eg, accept (N + 1) × 2 eg, do not accept N + 1 × 2
1m	Completes two rules correctly	

Tier & Question 3-5 4-6 5-7 6-8 25 14 9		Correct response	Fortieths
23 10 0	IVIALK	Correct response	Additional guidance
	1m	0.775	× Equivalent fractions
	1m	0.575	 ✓ Follow-through as their value for the first mark – 0.2

		Ωuesti				Furnerations
3–5		5–7 17		Mark	Correct response	Expressions Additional guidance
						-
	a	a	a	1m	 Indicates 2n must be even and gives a correct explanation eg Any whole number multiplied by two gives a number in the two times table, so is even Odd × 2 = even, even × 2 = even 2 × odd is odd + odd = even 2 × even is even + even = even All multiples of 2 are even Halving an odd number does not give a whole number 	 Minimally acceptable explanation eg × 2 gives even Doubling any number gives even All the numbers in the 2 times table are even Incomplete explanation eg 2 × 1 = 2 which is even, and 2 × 2 = 4 which is also even Even × even is even
	Ь	Ь	Ь	1m	 Indicates 3n could be odd or even and gives a correct explanation eg 3 × 1 = 3 which is odd, but 3 × 2 = 6 which is even Odd × 3 = odd, even × 3 = even Multiples of 3 can be odd or even An even or odd number can have a factor of 3 	 ✓ Minimally acceptable explanation eg 3 × 1 = 3, 3 × 2 = 6 If n is 5 you get odd, if n is 6, you get even 3 × some numbers = odd, but

3–5	4–6	2uesti 5–7 18	6–8	Mark	Correct response	Ratio Additional guidance
		а	а	1m	8	
		b	b	1m (U1)	Gives a correct number of black beads and white beads such that: the number of black beads is $(3n - 1)$ and the number of white beads is $(2n - 3)$, provided $n \ge 2$ eg • 5 black beads, 1 white bead • 8 black beads, 3 white beads • 11 black beads, 5 white beads	Markers may find the following list of correct examples helpful:BlackWhite51831151471792011

Tier & Question 3-5 4-6 5-7 6-8 28 19 11 Mark	Correct response	Powers Additional guidance
1m	Gives a correct justification that the difference between 3^2 and 3^3 is 18 eg • $3^2 = 9$, $3^3 = 27$, and $27 - 9 = 18$ • $3^3 - 3^2 = 3^2(3 - 1)$ = 9×2 = 18	 ✓ Minimally acceptable justification eg 27 - 9 9 + 18 = 27 ✓ Incomplete or incorrect justification eg 3² = 9, 3³ = 27 3³ - 3² = 18 9 - 27 = 18

Tier & Question 3–5 4–6 5–7 6–8			Sorting primes
		Correct response	Additional guidance
	1m	Identifies a value, <i>n</i> , such that <i>n</i> is prime, and shows that 2 <i>n</i> + 1 is not prime to demonstrate that the statement is incorrect eg • 7 is a prime number, but 2 × 7 + 1 = 15, and 15 is not a prime number • 13 is prime, but 27 is not	✓ Minimally acceptable response eg • 7, 15 • $2 \times 13 + 1 = 27$ ✓ Incomplete or incorrect response eg • $2 \times n$ is even, even + 1 is odd and not all odd numbers are prime ! More than one example given Accept provided a counter example is clearly identified eg, accept • 11 gives 23 13 gives 27 so this one eg, do not accept • 11 gives 23 13 gives 27 Markers may find the following list of correct examples helpful ($n < 100$): $\overline{n 2n + 1}$ 7 15 13 27 17 35 19 39 31 63 37 75 43 87 47 95 59 119 61 123 67 135 71 143 73 147 79 159 97 195

Tier & Question 3–5 4–6 5–7				Score
		Mark	Correct response	Additional guidance
а	а	2m or 1m	11 Shows the values 56 and 45 or Gives an answer of 9 [the points gained in round 5]	
b	b	1m	 Gives a response that states or implies that Derek gained the same number of points in each round eg He got the same number of points in each round To keep the gradient the same, an equal number needs to be added each time For every round going across, the line must have gone up the graph in equal steps 	 Minimally acceptable response eg eg Same Equal No change The total increases by the same number in each round He gained 10 points each round He gained 10 points each round He gets about the same number of points in each round It increases by the same number in each round It increases by the same number in each round He gets about the same number of points in each round It increases by the same number in each round His points were consistent A steady increase He gets maximum points each round The line could be horizontal

Tier & Ques 5 4–6 5–7 22	7 6–8	Mark	Correct response	Rhombus Additional guidance
		2m or 1m	 24 Shows a correct method with not more than one computational error The most common correct methods: Calculate the area of the rhombus as half the area of the rectangle eg 1/2 (6 × 8) 48 ÷ 2 Work with 2 or 4 triangles eg Area of one little triangle is half of 3 × 4, there are 4 little triangles so × 4 (6 × 4) ÷ 2 = 14 (error), 14 × 2 = 28 8 triangles altogether, so one is 48 ÷ 8 = 7 (error), 4 shaded so 4 × 7 = 28 Area of rectangle: 6 × 8 = 48, Area of white triangle: 1/2 × 3 × 4 = 6 4 × 6 = 18 (error), answer 30 	 Conceptual error eg Area of triangle given as base × height
		1m	Shows the correct unit for their area or method eg • 24cm ² • 2400mm ²	! Area incorrect or omitted, but units given If the mark(s) for the correct area have not been awarded, condone cm ² seen for the third mark

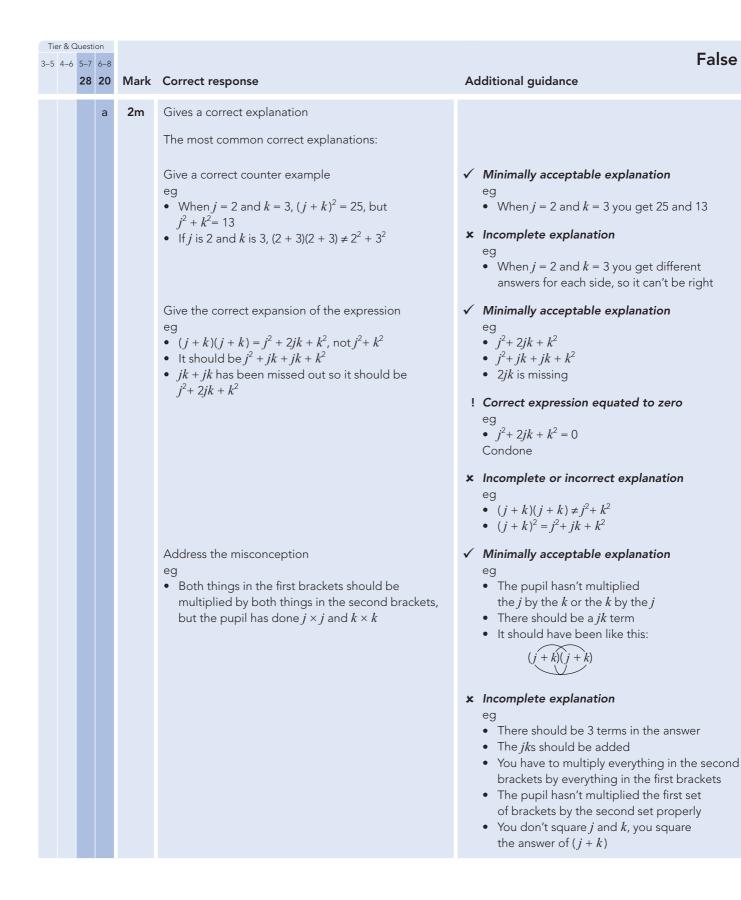
Tier & 3–5 4–6	5–7		Mark	Correct response	Sums and products Additional guidance
	а	а	1m	Gives a pair of values with a negative sum and a positive product, ie where a and b are both negative eg • -2 and -1 • -9 and -10 • -0.5 and $-\frac{2}{5}$ • -3 and -3	
	b	b	1m	Gives a pair of values with a positive sum and a negative product, ie where <i>a</i> is positive, <i>b</i> is negative and $ a > b $ eg • 2 and -1 • -9 and 10 • 0.5 and $-\frac{2}{5}$	

Tier & Question 3-5 4-6 5-7 6-8 24 16 Mark	Correct response	Mean Additional guidance
2m or 1m	16 Shows the value 66 or Shows or implies a complete correct method with not more than one computational error eg • $6 \times 11 - 5 \times 10$ • $5 \times 10 = 50, 6 \times 11 = 65$ (error) so 15	 For 1m, method uses arbitrary values with a mean of 10 for the original five numbers Condone eg, for 1m accept 8 + 9 + 10 + 11 + 12 = 49 (error) 6 × 11 - 49 = 17 For 1m, error is in the number of values in the set after one is added eg 5 × 11 = 55, 55 - 50 = 5

Tier & Question 3-5 4-6 25 17	Mark	Correct response	Simultaneous Additional guidance
	or 2m	Gives both $x = 5$ and $y = \frac{5}{2}$ or equivalent and shows or implies a complete correct method for solving algebraically eg • $2x = 10, x = 5$ and $y = \frac{5}{2}$ • $3x + 18y = 60$ 3x + 6y = 30 12y = 30, so $y = 2.5$ and $x = 5• 30 - 3x = 20 - x10 = 2x, x = 5$ and $y = 2.5• 3(20 - 6y) + 6y = 3060 - 18y + 6y = 3030 = 12y, y = 2.5$ and $x = 5Gives either x = 5 or y = \frac{5}{2} or equivalent andshows or implies a correct method for solvingalgebraically for that variableeg• 2x = 10, x = 5• 3x + 18y = 603x + 6y = 3012y = 30$, so $y = 2.5• 30 - 3x = 20 - x10 = 2x, x = 5• 3(20 - 6y) + 6y = 3060 - 18y + 6y = 30$	 Method used is trial and improvement
	or	30 = 12y, y = 2.5	
	or 1m	Subtracts the two given equations to eliminate y, or forms two correct equations that would allow elimination of x eg • $2x = 10$ • $3x + 18y = 60$ 3x + 6y = 30 or Attempts to solve by substitution and forms a correct equation in only one variable eg • $3(20 - 6y) + 6y = 30$ • $x + 30 - 3x = 20$	

Tier & Question 3-5 4-6 5-7 6-8 26 18 Mark	Correct response	Shape Additional guidance
2m or 1m	200, with no evidence of an incorrect method Shows or implies that $a = 5$ or Shows or implies that the area of one rectangle is 50 or Shows a complete correct method with not more than one computational error eg • $16a = 80$, so $a = 6$ (error) $6 \times 12 = 72$, $72 \times 4 = 288$! Error made in coefficient of a Follow-through with this value provided $12 \le \text{coefficient of } a \le 20$ eg • $12a (error) = 80$, so $a = 6.6$ $6.6 \times 13.2 \times 4 = 348$

Tier & Question 3-5 4-6 5-7 6-8			Circle shapes
27 19	Mark	Correct response	Additional guidance
	1m	Gives the correct expression for area A, ie Area A = $y + 3w$	 Inroughout the question, unconventional notation or unsimplified expressions Condone eg, for Area A, accept y + 3 × w y + w + w + w eg, for Area B, accept 1y + 1w y + 3w - 2w
	1m (U1)	Gives the correct expression for area B, ie Area B = $y + w$! Answers for Area A and Area B transposed but otherwise correct Mark as 0, 1 ! Answers for Area A and Area B correct followed by incorrect further processing Mark as 0, 1



Tier & Question 3-5 4-6 5-7 6-8 28 20	Mark	Correct response	Additional guidance	False (cont)
	or 1m	Shows a complete correct method with not more than one computational error when substituting values eg • If $j = 2$ and $k = 3$ $(j + k)^2 = (2 + 3)^2 = 20$ (error), $j^2 + k^2 = 4 + 9 = 13$ or Shows or implies the four correct terms resulting from multiplying out the brackets, even if there is incorrect further working eg • j^2 , jk , jk , k^2 • $j \times j + j \times k + j \times k + k \times k$	 Conceptual error eg 3² = 6 	
b	1m	 Gives a correct counter example g j = 0 k = 0 Either j or k is zero Both j and k are zero It doesn't work if k is nought 		



	21 M	lark	Correc	ct res	ponse					Additional guidance	Dice probability
		2m or	$\frac{3}{4}$ or eq	quival	ent pro	bability					
		lm	Shows or implies the number of possible outcomes where the product is a multiple of 3 eg						outcomes		
			•	×	3	4	5	6			
				3	<u>9</u>	<u>12</u>	<u>15</u>	<u>18</u>	-		
				4	<u>12</u>	16	20	<u>24</u>			
				5	<u>15</u>	20	25	<u>30</u>			
				6	<u>18</u>	<u>24</u>	<u>30</u>	<u>36</u>			
			•		3	4	5	6]		
			-	3		 ✓	√	√			
				4	\checkmark			✓			
				5	\checkmark			\checkmark			
				6	\checkmark	\checkmark	\checkmark	\checkmark			
	• $3 \times 3, 3 \times 4, 3 \times 5, 3 \times 6,$ $4 \times 3, 4 \times 6,$ $5 \times 3, 5 \times 6,$ $6 \times 3, 6 \times 4, 6 \times 5, 6 \times 6$										
			or								
			more t then fo	than t	wo erro	ors in ide	entifying	, multipl	kes not les of 3, probability		
			•	×	3	4	5	6			
				3	<u>9</u>	<u>12</u>	<u>15</u>	<u>18</u>			
				4	<u>12</u>	16	20	<u>24</u>	-		
				5	15	20	25	<u>30</u>	-		
				6	<u>18</u>	<u>24</u>	<u>30</u>	<u>36</u>			
	l	J2)						so <u>11</u> 16			

Tier & Question 3–5 4–6 5–7 6				Solving
;	22	Mark	Correct response	Additional guidance
		2m or 1m	Gives $y = 20$ and shows or implies a correct first step of algebraic manipulation that either removes the denominator or removes the brackets eg • $5(3y - 4) = 14y$ • $5(3y - 4) = 14y$ • $5(3y - 4) = 2y \times 7$ • $\frac{15y - 20}{2y} = 7$ • $\frac{5 \times 3y - 5 \times 4}{2y} = 7$ • $15y - 20 = 14y$ • $y - 20 = 0$ Shows or implies a correct first step of algebraic manipulation that either removes the denominator or removes the brackets, even if there are other errors	
		2m or 1m	Gives $x = 5$ and $x = -5$, in either order and shows or implies the correct expansion of (x + 4)(x - 4) eg • $x^2 + 4x - 4x - 16$ • $x 4$ $x x^2 4x$ -4 -4x -16 • $x^2 - 16$ • $x^2 = 25$ Shows or implies the correct expansion of (x + 4)(x - 4), even if there are other errors	

Tier & Question			
3-5 4-6 5-7 6-	-8	Marking overlay available	Distance from school
2	3 Mark	Correct response	Additional guidance
đ	a 2m or 1m	 Draws a correct graph within the tolerance as shown on the overlay that fulfils the following conditions: 1. All four points marked correctly, ie (2, 19), (3, 25), (4, 28) and (5, 29) 2. All points joined with a series of straight lines Shows or implies the values 19, 25, 28 and 29 eg Fulfils condition 1 only Marks the points (1.5, 19), (2.5, 25), (3.5, 28) and (4.5, 29) [ie uses midpoints of each range as <i>x</i>-coordinates] or Marks and joins at least three points correctly or 	! For 2m or 1m, points joined with a curve Condone
	U2	Makes an error in marking one of the points, but follows through correctly for later points, and joins all their points	I Follow-throughFor 1m, accept the following values as follow-through:DistanceCff-t219none3256 + their 194283 + their 255291 + their 28
k	5 1m	Gives a value between 1.4 and 1.6 inclusive or Follows through from an incorrect total to give the correct median for their graph	 ✓ Equivalent fractions or decimals ! Follow-through Follow-through can only be given for an increasing graph which reaches (5, y)
Tier & Question			
3–5 4–6 5–7 6-		Marking overlay available	Coordinates
2	4 Mark	Correct response	Additional guidance
	1m 1m	Gives A as (0, –2) Gives B as (1, –1)	! Answers for A and B transposed but otherwise completely correct If this is the only error, ie gives A as (1, -1) and gives B as (0, -2), mark as 0, 1

Tier & Question 3-5 4-6 5-7 6-8 25 25		Correct response	Similar triangles
	2m <i>or</i> 1m	 3, with no evidence of accurate or scale drawing Shows or implies the ratio 4 : 10 eg 0.4 or equivalent seen 2.5 or equivalent seen 2 : 5 = ? : 7¹/₂ 7.5 ÷ 10 × 4 0.75 × 4 30 ÷ 10 	For 2m or 1m, evidence of accurate or scale drawing, with no other method
Tier & Question 3–5 4–6 5–7 6–8			Regions
26		Correct response	Additional guidance
а	1m	Gives the four correct letters, ie A. B. G and H. in any order	

		A, B, G and H, in any order
b	1m	Gives the four correct letters, ie B, C, D and E, in any order
с	1m	Gives the four correct letters, ie A, B, E and F, in any order

Tier & Question 3–5 4–6 5–7 6–8 27		Correct response	Average speed
27	WIDIK	Correct response	Additional guidance
	2m	Gives a correct justification that the average speed is 20km per hour eg • 1km at 15km/h takes 60 ÷ 15 = 4 minutes, 1km at 30km/h takes 60 ÷ 30 = 2 minutes, 2km in 6 minutes = 20km in 60 minutes = 20km per hour • $\frac{1}{15} + \frac{1}{30} = \frac{3}{30}$ $= \frac{1}{10}$, 2km in $\frac{1}{10}$ hour = 20km in 1 hour	 ✓ For 2m, minimally acceptable justification eg • 4 + 2 = 6 mins for 2km • 1/15 + 1/30 = 1/10 for 2km ✓ For 2m, incomplete justification eg • 1km at 15km per hour takes 60 ÷ 15 = 4 mins, 1km at 30km per hour takes 60 ÷ 30 = 2 mins • 6 mins for 2km, so it's 60 mins for 20km which is 20km per hour
	or		
	1m	 Shows or implies that the journey time up the hill was 4 minutes or equivalent, and the journey time down the hill was 2 minutes or equivalent eg 4, 2 seen ¹/₁₅, ¹/₃₀ seen 60 ÷ 15, 60 ÷ 30 seen 	! For 1m, total of 6 minutes or equivalent seen As the total of 6 minutes can be calculated from the given 20km per hour, do not accept as implying 4 minutes and 2 minutes unless a correct method is also seen

Index to mark schemes

	Ti	er		Question	Page
3–5	4–6	5–7	6–8		
1				Circle totals	10
2				Dishes	11
3				Five squares	12
4				Javelin	12
5				Digit cards	13
6				Heights	13
7				Change	14
8	1			Doctors	14
9	2			Using tens	15
10	3			Card shape	15
11	4			Number lines	15
12	5			Rhombus grid	16
13	6			Missing digits	17
14	7			Clocks	17
15	8			Sum of 80	18
16	9			Number chains	18
17	10	1		Making 1	19
18	11	2		T-shirts	19
19	12	3		Water	20
20	13	4		Boxes	20
21	14	5		Percentages	20
22	15	6		Number grids	21
23	16	7		Angles in a triangle	21
24	17	8		Finding <i>b</i>	22

	Ti	er		Question	Page
3–5	4–6	5–7	6–8		
	18	9	1	Matching	22
	19	10	2	Oak leaves	23
	20	11	3	Missing lengths	24
	21	12	4	Counters	25
	22	13	5	Prize money	25
	23	14	6	Correlation	26
	24	15	7	Shape rules	27
	25	16	8	Fortieths	27
	26	17	9	Expressions	28
	27	18	10	Ratio	29
	28	19	11	Powers	29
		20	12	Sorting primes	30
		21	13	Score	31
		22	14	Rhombus	32
		23	15	Sums and products	33
		24	16	Mean	33
		25	17	Simultaneous	34
		26	18	Shape	35
		27	19	Circle shapes	35
		28	20	False	36
			21	Dice probability	38
			22	Solving	39
			23	Distance from school	40
			24	Coordinates	40
			25	Similar triangles	41
			26	Regions	41
			27	Average speed	41



QCA wishes to make its publications widely accessible. Please contact us if you have any specific accessibility requirements. 29 Bolton Street London W1J 8BT

Telephone: 08700 60 60 40 Minicom: 020 7509 6546 Fax: 020 7509 5908

Email: tests@naa.org.uk Website: www.naa.org.uk/tests

First published 2009

© Qualifications and Curriculum Authority 2009

ISBN 1-84721-699-1

Reproduction, storage, adaptation or translation, in any form or by any means, of this publication is prohibited without prior written permission of the publisher, unless within the terms of licences issued by the Copyright Licensing Agency. Excerpts may be reproduced for the purpose of research, private study, criticism or review, or by educational institutions solely for educational purposes, without permission, providing full acknowledgement is given.

Printed in Great Britain by the Qualifications and Curriculum Authority under the authority and superintendence of the Controller of Her Majesty's Stationery Office and Queen's Printer of Acts of Parliament.

The Qualifications and Curriculum Authority is an exempt charity under Schedule 2 of the Charities Act 1993.

Qualifications and Curriculum Authority 83 Piccadilly London W1J 8QA www.qca.org.uk



Qualifications and

For more copies: QCA Orderline, PO Box 29, Norwich NR3 1GN www.qca.org.uk/orderline email: orderline@qca.org.uk Tel: 08700 60 60 15 Fax: 08700 60 60 17

Cursiculter AuthSAity-Papers.co.uRCA/09/3783

https://www.SATs-Papers.co.uk²⁹⁰⁰¹⁵